



IJEAST

INTERNATIONAL JOURNAL
OF ENGINEERING APPLIED SCIENCE
AND TECHNOLOGY



VOLUME : 4 ISSUE : 01 Print / Issue Publication Date: 27-Jun-2019



ISSN : 2455-2143



DOI : 10.33564/IJEAST.2019.v04i01.005

Indexed In



WWW.IJEAST.COM

editor@ijeast.com



A NOTE ON INTUITIONISTIC FUZZY β GENERALIZED IRRESOLUTE MAPPINGS

R.Kulandaivelu

Department of Mathematics
Dr. N.G.P. Institute of Technology,
Coimbatore, Tamilnadu, India

S.Maragathavalli

Department of Mathematics
Government Arts College,
Udumalpet, Tamilnadu, India

K. Ramesh

Department of Mathematics
CMS College of Engineering and Technology,
Coimbatore, Tamilnadu, India

ABSTRACT: In this paper a new class of mapping called intuitionistic fuzzy β generalized irresolute mapping in intuitionistic fuzzy topological space is introduced and its properties are studied. Further the notion of intuitionistic fuzzy $\beta_{aT_{1/2}}$ space and intuitionistic fuzzy $\beta_{bT_{1/2}}$ are introduced.

KEYWORDS: Intuitionistic fuzzy topology, intuitionistic fuzzy β generalized closed set, intuitionistic fuzzy β generalized open set, intuitionistic fuzzy β generalized irresolute mapping, intuitionistic fuzzy contra β generalized irresolute mapping, intuitionistic fuzzy $\beta_{aT_{1/2}}$ space and intuitionistic fuzzy $\beta_{bT_{1/2}}$ space.

AMS SUBJECT CLASSIFICATION (2000):54A40, 03F55

I. INTRODUCTION

After the introduction of Fuzzy set (FS) by Zadeh [12] in 1965 and fuzzy topology by Chang [3] in 1967, several researches were conducted on the generalizations of the notions of fuzzy sets and fuzzy topology. The concept of intuitionistic fuzzy set (IFS) was introduced by Atanassov in 1983 as a generalization of fuzzy sets. In 1997 Coker [4] introduced the concept of intuitionistic fuzzy topological space. In this paper we introduce the notion of intuitionistic fuzzy β generalized irresolute mappings, intuitionistic fuzzy contra β generalized irresolute mapping in intuitionistic fuzzy topological space and studied some of their properties. We provide some characterizations of intuitionistic fuzzy β generalized irresolute mappings, intuitionistic fuzzy contra β generalized irresolute mappings and established the relationships with other classes of early defined forms of intuitionistic fuzzy mappings.

II. PRELIMINARIES

Definition 2.1: [1] Let X be a non empty fixed set. An intuitionistic fuzzy set (IFS in short) A in X is an object having the form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle / x \in X \}$$

where the functions $\mu_A(x): X \rightarrow [0, 1]$ and $\nu_A(x): X \rightarrow [0, 1]$ denote the degree of membership (namely $\mu_A(x)$) and the degree of non-membership (namely $\nu_A(x)$) of each element $x \in X$ to the set A , respectively, and $0 \leq \mu_A(x) + \nu_A(x) \leq 1$ for each $x \in X$. Denote the set of all intuitionistic fuzzy sets in X by $\text{IFS}(X)$.

Definition 2.2: [1] Let A and B be IFSs of the form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle / x \in X \} \text{ and } B = \{ \langle x, \mu_B(x), \nu_B(x) \rangle / x \in X \}.$$

(a) $A \subseteq B$ if and only if $\mu_A(x) \leq \mu_B(x)$ and $\nu_A(x) \geq \nu_B(x)$ for all $x \in X$

(b) $A = B$ if and only if $A \subseteq B$ and $B \subseteq A$

(c) $A^c = \{ \langle x, \nu_A(x), \mu_A(x) \rangle / x \in X \}$

(d) $A \cap B = \{ \langle x, \mu_A(x) \wedge \mu_B(x), \nu_A(x) \vee \nu_B(x) \rangle / x \in X \}$

(e) $A \cup B = \{ \langle x, \mu_A(x) \vee \mu_B(x), \nu_A(x) \wedge \nu_B(x) \rangle / x \in X \}$

For the sake of simplicity, we shall use the notation $A = \langle x, \mu_A, \nu_A \rangle$ instead of $A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle / x \in X \}$. Also for the sake of simplicity, we shall use the notation $A = \langle x, (\mu_A, \mu_B), (\nu_A, \nu_B) \rangle$ instead of $A = \langle x, (A/\mu_A, B/\mu_B), (A/\nu_A, B/\nu_B) \rangle$.

The intuitionistic fuzzy sets $0 \sim = \{ \langle x, 0, 1 \rangle / x \in X \}$ and $1 \sim = \{ \langle x, 1, 0 \rangle / x \in X \}$ are respectively the empty set and the whole set of X .

Definition 2.3: [3] An intuitionistic fuzzy topology (IFT in short) on X is a family τ of IFSs in X satisfying the following axioms.

(i) $0 \sim, 1 \sim \in \tau$

(ii) $G_1 \cap G_2 \in \tau$ for any $G_1, G_2 \in \tau$

(iii) $\cup G_i \in \tau$ for any family $\{ G_i / i \in J \} \subseteq \tau$.



In this case the pair (X, τ) is called an intuitionistic fuzzy topological space (IFTS in short) and any IFS in τ is known as an intuitionistic fuzzy open set (IFOS in short) in X .

The complement A^c of an IFOS A in IFTS (X, τ) is called an intuitionistic fuzzy closed set (IFCS in short) in X .

Definition 2.4:[3] Let (X, τ) be an IFTS and $A = \langle x, \mu_A, \nu_A \rangle$ be an IFS in X . Then the intuitionistic fuzzy interior and intuitionistic fuzzy closure are defined by

$$\text{int}(A) = \bigcup \{ G / G \text{ is an IFOS in } X \text{ and } G \subseteq A \},$$

$$\text{cl}(A) = \bigcap \{ K / K \text{ is an IFCS in } X \text{ and } A \subseteq K \}$$

Note that for any IFS A in (X, τ) , we have $\text{cl}(A^c) = [\text{int}(A)]^c$ and $\text{int}(A^c) = [\text{cl}(A)]^c$.

Definition 2.5: [4] An IFS $A = \langle x, \mu_A, \nu_A \rangle$ in an IFTS (X, τ) is said to be a

(i) intuitionistic fuzzy semi closed set (IFSCS for short) if $\text{int}(\text{cl}(A)) \subseteq A$,

(ii) intuitionistic fuzzy pre-closed set (IFPCS for short) if $\text{cl}(\text{int}(A)) \subseteq A$,

(iii) intuitionistic fuzzy α -closed set (IF α CS for short) if $\text{cl}(\text{int}(\text{cl}(A))) \subseteq A$,

(iv) intuitionistic fuzzy γ -closed set (IF γ CS for short) if $\text{cl}(\text{int}(A)) \cap \text{int}(\text{cl}(A)) \subseteq A$

The respective complements of the above IFCSs are called their respective IFOSs.

The family of all IFSCSs, IFPCSs, IF α CSs and IF γ CSs (respectively IFSOSs, IFPOSs, IF α OSs and IF γ OSs) of an IFTS (X, τ) are respectively denoted by IFSC(X), IFPC(X), IF α C(X) and IF γ C(X) (respectively IFSO(X), IFPO(X), IF α O(X) and IF γ O(X)).

Definition 2.6:[11] Let A be an IFS in an IFTS (X, τ) . Then

$$\text{sint}(A) = \bigcup \{ G / G \text{ is an IFSOS in } X \text{ and } G \subseteq A \},$$

$$\text{scl}(A) = \bigcap \{ K / K \text{ is an IFSCS in } X \text{ and } A \subseteq K \}.$$

Note that for any IFS A in (X, τ) , we have $\text{scl}(A^c) = (\text{sint}(A))^c$ and $\text{sint}(A^c) = (\text{scl}(A))^c$.

Definition 2.7:[10] An IFS A in an IFTS (X, τ) is an intuitionistic fuzzy generalized closed set (IFGCS in short) if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is an IFOS in X .

Definition 2.8:[10] An IFS A in an IFTS (X, τ) is said to be an intuitionistic fuzzy generalized semi closed set (IFGSCS in short) if $\text{scl}(A) \subseteq U$ whenever $A \subseteq U$ and U is an IFOS in (X, τ) .

Definition 2.9:[10] An IFS A is said to be an intuitionistic fuzzy generalized semi open set (IFGSOS in short) in X if the complement A^c is an IFGSCS in X .

The family of all IFGSCSs (IFGSOSs) of an IFTS (X, τ) is denoted by IFGSC(X) (IFGSO(X)).

Definition 2.10:[5] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be intuitionistic fuzzy

continuous (IF continuous in short) if $f^{-1}(B) \in \text{IFO}(X)$ for every $B \in \sigma$.

Definition 2.11: [5] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be an

- (i) intuitionistic fuzzy semi continuous mapping (IFS continuous mapping for short) if $f^{-1}(B) \in \text{IFSO}(X)$ for every $B \in \sigma$
- (ii) intuitionistic fuzzy α -continuous mapping (IF α continuous mapping for short) if $f^{-1}(B) \in \text{IF}\alpha\text{O}(X)$ for every $B \in \sigma$
- (iii) intuitionistic fuzzy pre continuous mapping (IFP continuous mapping for short) if $f^{-1}(B) \in \text{IFPO}(X)$ for every $B \in \sigma$
- (iv) intuitionistic fuzzy γ continuous mapping (IF γ continuous mapping for short) if $f^{-1}(B) \in \text{IF}\gamma\text{O}(X)$ for every $B \in \sigma$.

Definition 2.12: [11] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be an intuitionistic fuzzy generalized continuous mapping (IFG continuous mapping for short) if $f^{-1}(B) \in \text{IFGC}(X)$ for every IFCS B in Y .

Definition 2.13: [11] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be an intuitionistic fuzzy semi-pre continuous mapping (IFSP continuous mapping for short) if $f^{-1}(B) \in \text{IFSPO}(X)$ for every $B \in \sigma$.

Result 2.14:[8] Every IF continuous mapping is an IFG continuous mapping.

Definition 2.15:[8] A mapping $f: (X, \tau) \rightarrow (Y, \sigma)$ is called an intuitionistic fuzzy generalized semi continuous (IFGS continuous in short) if $f^{-1}(B)$ is an IFGSCS in (X, τ) for every IFCS B of (Y, σ) .

Definition 2.16: [8] An IFTS (X, τ) is said to be an intuitionistic fuzzy $\beta_{aT1/2}$ (IF $\beta_{aT1/2}$ in short) space if every IF $\beta_{aT1/2}$ GCS in X is an IFCS in X .

Definition 2.17: [8] An IFTS (X, τ) is said to be an intuitionistic fuzzy $\beta_{bT1/2}$ (IF $\beta_{bT1/2}$ in short) space if every IF $\beta_{bT1/2}$ GCS in X is an IFGCS in X .

Definition 2.18:[9] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be an intuitionistic fuzzy irresolute (IF irresolute in short) if $f^{-1}(B) \in \text{IFCS}(X)$ for every IFCS B in Y .

Definition 2.19:[9] Let f be a mapping from an IFTS (X, τ) into an IFTS (Y, σ) . Then f is said to be an intuitionistic fuzzy generalized irresolute (IFG irresolute in short) if $f^{-1}(B) \in \text{IFGCS}(X)$ for every IFGCS B in Y .



III. INTUITIONISTIC FUZZY GENERALIZED IRRESOLUTE MAPPINGS

In this section, we have introduced intuitionistic fuzzy generalized irresolute mappings and studied some of their properties.

Definition 3.1: A mapping $f : (X, \tau) \rightarrow (Y, \sigma)$ is called an intuitionistic fuzzy generalized irresolute (IFG irresolute) mapping if $f^{-1}(A)$ is an IFGCS in (X, τ) for every IFGCS A of (Y, σ) .

Theorem 3.2: If $f : (X, \tau) \rightarrow (Y, \sigma)$ is an IFG irresolute mapping, then f is an IFG continuous mapping but not conversely.

Proof: Assume that f is an IFG irresolute mapping. Let A be any IFCS in Y . Since every IFCS is an IFGCS, A is an IFGCS in Y . By hypothesis $f^{-1}(A)$ is an IFGCS in X . Hence f is an IFG continuous mapping.

Example 3.3: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $G_1 = \langle x, (0.1, 0.3), (0.6, 0.3) \rangle$, $G_2 = \langle y, (0.3, 0.1), (0.5, 0.6) \rangle$. Then $\tau = \{0_\sim, G_1, 1_\sim\}$ and $\sigma = \{0_\sim, G_2, 1_\sim\}$ are IFTs on X and Y respectively. Define a mapping $f : (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. Then f is an IFG continuous mapping. Let $B = \langle y, (0.1, 0.1), (0.6, 0.4) \rangle$ is an IFGCS in Y . But $f^{-1}(B) = \langle x, (0.1, 0.1), (0.6, 0.4) \rangle$ is not an IFGCS in X . Therefore, f is not an IFG irresolute mapping.

Theorem 3.4: If $f : (X, \tau) \rightarrow (Y, \sigma)$ is an IFG irresolute mapping, then f is an IFGS continuous mapping but not conversely.

Proof: Assume that f is an IFG irresolute mapping. Let A be any IFCS in Y . Since every IFCS is an IFGCS, A is an IFGCS in Y . By hypothesis $f^{-1}(A)$ is an IFGCS in X . This implies $f^{-1}(A)$ is an IFGCS in X . Hence f is an IFGS continuous mapping.

Example 3.5: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $G_1 = \langle x, (0.1, 0.3), (0.3, 0.3) \rangle$, $G_2 = \langle y, (0.3, 0.1), (0.4, 0.4) \rangle$. Then $\tau = \{0_\sim, G_1, 1_\sim\}$ and $\sigma = \{0_\sim, G_2, 1_\sim\}$ are IFTs on X and Y respectively. Define a mapping $f : (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. Then f is an IFGS continuous mapping. Let $B = \langle y, (0.1, 0.1), (0.3, 0.4) \rangle$ is an IFGCS in Y . But $f^{-1}(B) = \langle x, (0.1, 0.1), (0.3, 0.4) \rangle$ is not an IFGCS in X . Therefore, f is not an IFG irresolute mapping.

Theorem 3.6: If $f : (X, \tau) \rightarrow (Y, \sigma)$ is an IFG irresolute mapping in an $IF_{aT_{1/2}}$ space X , then f is an IF continuous mapping.

Proof: Let A be an IFCS in Y . Then A is an IFGCS in Y . Since f is an IFG irresolute, $f^{-1}(A)$ is an IFGCS in X . Also, since X is an $IF_{aT_{1/2}}$ space, $f^{-1}(A)$ is an IFCS in X . Hence f is an IF continuous mapping.

Theorem 3.7: Let $f : (X, \tau) \rightarrow (Y, \sigma)$ and $g : (Y, \sigma) \rightarrow (Z, \eta)$ be IFG irresolute mappings. Then $g \circ f : (X, \tau) \rightarrow (Z, \eta)$ is an IFG irresolute mapping.

Proof: Let A be an IFGCS in Z . Then by hypothesis, $g^{-1}(A)$ is an IFGCS in Y . Since f is an IFG irresolute mapping, $f^{-1}(g^{-1}(A))$ is an IFGCS in X . Thus, $(g \circ f)^{-1}(A)$ is an IFGCS in X . Therefore $g \circ f$ is an IFG irresolute mapping.

Theorem 3.8: Let $f : (X, \tau) \rightarrow (Y, \sigma)$ be an IFG irresolute mapping and $g : (Y, \sigma) \rightarrow (Z, \eta)$ be an IFG continuous mapping. Then $g \circ f : (X, \tau) \rightarrow (Z, \eta)$ is an IFG continuous mapping.

Proof: Let A be an IFCS in Z . Then by hypothesis, $g^{-1}(A)$ is an IFGCS in Y . Since f is an IFG irresolute mapping, $f^{-1}(g^{-1}(A))$ is an IFGCS in X . Thus, $(g \circ f)^{-1}(A)$ is an IFGCS in X .

Therefore, $g \circ f$ is an IFG continuous mapping.

Theorem 3.9: If $f : (X, \tau) \rightarrow (Y, \sigma)$ is an IFG irresolute mapping in an $IF_{bT_{1/2}}$ space in X , then f is an IFG irresolute mapping.

Proof: Let A be an IFGCS in Y . Then A is an IFGCS in Y . Therefore $f^{-1}(A)$ is an IFGCS in X , by hypothesis. Since X is an $IF_{bT_{1/2}}$ space, $f^{-1}(A)$ is an IFGCS in X . Hence f is an IFG irresolute mapping.

Theorem 3.10: Let $f : (X, \tau) \rightarrow (Y, \sigma)$ be a mapping from an IFTS X into an IFTS Y . Then the following conditions are equivalent if X and Y are $IF_{aT_{1/2}}$ spaces:

- (i) f is an IFG irresolute mapping
- (ii) $f^{-1}(B)$ is an IFGOS in X for each IFGOS in Y
- (iii) $cl(f^{-1}(B)) \subseteq f^{-1}(cl(B))$ for each IFS B of Y .

Proof: (i) $\Rightarrow$ (ii): Obviously true.

(ii) $\Rightarrow$ (iii): Let B be any IFS in Y . Clearly $B \subseteq cl(B)$. Then $f^{-1}(B) \subseteq f^{-1}(cl(B))$. Since $cl(B)$ is an IFCS in Y , $cl(B)$ is an IFGCS in Y . Therefore, $f^{-1}(cl(B))$ is an IFGCS in X , by hypothesis. Since X is an $IF_{aT_{1/2}}$ space, $f^{-1}(cl(B))$ is an IFCS



in X . Hence $\text{cl}(f^{-1}(B)) \subseteq \text{cl}(f^{-1}(\text{cl}(B))) = f^{-1}(\text{cl}(B))$. That is $\text{cl}(f^{-1}(B)) \subseteq f^{-1}(\text{cl}(B))$.

(iii) $\Rightarrow$ (i): Let B be an $\text{IF}_{\beta}^{\text{GCS}}$ in Y . Since Y is an $\text{IF}_{\beta}^{\text{aT}_{1/2}}$ space, B is an IFCS in Y and $\text{cl}(B) = B$. Hence $f^{-1}(B) = f^{-1}(\text{cl}(B)) \supseteq \text{cl}(f^{-1}(B))$, by hypothesis. But clearly $f^{-1}(B) \subseteq \text{cl}(f^{-1}(B))$. Therefore, $\text{cl}(f^{-1}(B)) = f^{-1}(B)$. This implies $f^{-1}(B)$ is an IFCS in X and hence it is an $\text{IF}_{\beta}^{\text{GCS}}$ in X . Thus f is an $\text{IF}_{\beta}^{\text{G}}$ irresolute mapping.

IV. INTUITIONISTIC FUZZY CONTRA GENERALIZED IRRESOLUTE MAPPINGS

In this section, we have introduced intuitionistic fuzzy contra generalized irresolute mapping and studied some of its properties.

Definition 4.1: A mapping $f : (X, \tau) \rightarrow (Y, \sigma)$ is called an intuitionistic fuzzy contra generalized irresolute (IFC $_{\beta}^{\text{G}}$ irresolute in short) mapping if $f^{-1}(A)$ is an $\text{IF}_{\beta}^{\text{GCS}}$ in (X, τ) for every $\text{IF}_{\beta}^{\text{GOS}}$ A of (Y, σ) .

Theorem 4.2: If $f : (X, \tau) \rightarrow (Y, \sigma)$ is an IFC $_{\beta}^{\text{G}}$ irresolute mapping, then f is an IFC $_{\beta}^{\text{G}}$ continuous mapping but not conversely.

Proof: Let f be an IFC $_{\beta}^{\text{G}}$ irresolute mapping. Let A be any IFCS in Y . Since every IFCS is an $\text{IF}_{\beta}^{\text{GCS}}$, A is an $\text{IF}_{\beta}^{\text{GCS}}$ in Y . By hypothesis $f^{-1}(A)$ is an $\text{IF}_{\beta}^{\text{GOS}}$ in X . Hence f is an IFC $_{\beta}^{\text{G}}$ continuous mapping.

Example 4.3: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $G_1 = \langle x, (0.1, 0.3), (0.6, 0.3) \rangle$, $G_2 = \langle y, (0.5, 0.6), (0.3, 0.1) \rangle$. Then $\tau = \{0., G_1, 1.\}$ and $\sigma = \{0., G_2, 1.\}$ are IFTs on X and Y respectively. Define a mapping $f : (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. Then f is an IFC $_{\beta}^{\text{G}}$ continuous mapping but f is not an IFC $_{\beta}^{\text{G}}$ irresolute mapping, since $B = \langle y, (0.1, 0.1), (0.6, 0.4) \rangle$ is an $\text{IF}_{\beta}^{\text{GOS}}$ in Y but $f^{-1}(B) = \langle x, (0.1, 0.1), (0.6, 0.4) \rangle$ is not an $\text{IF}_{\beta}^{\text{GCS}}$ in X .

Theorem 4.4: Let $f : (X, \tau) \rightarrow (Y, \sigma)$ be an IFC $_{\beta}^{\text{G}}$ irresolute mapping, then $f^{-1}(A)$ is an IFGSCS in X for every IFOS A in Y but not conversely.

Proof: Let f be an IFC $_{\beta}^{\text{G}}$ irresolute mapping. Let A be any IFOS in Y . Since every IFOS is an $\text{IF}_{\beta}^{\text{GOS}}$, A is an $\text{IF}_{\beta}^{\text{GOS}}$ in Y . By hypothesis, $f^{-1}(A)$ is an $\text{IF}_{\beta}^{\text{GCS}}$ in X . This implies $f^{-1}(A)$ is an IFGSCS in X .

Example 4.5: Let $X = \{a, b\}$, $Y = \{u, v\}$ and $G_1 = \langle x, (0.1, 0.3), (0.3, 0.3) \rangle$, $G_2 = \langle y, (0.4, 0.4), (0.3, 0.1) \rangle$. Then $\tau = \{0., G_1, 1.\}$ and $\sigma = \{0., G_2, 1.\}$ are IFTs on X and Y respectively. Define a mapping $f : (X, \tau) \rightarrow (Y, \sigma)$ by $f(a) = u$ and $f(b) = v$. Then $f^{-1}(A)$ is an IFGSCS in X for every IFOS A in Y . But f is not an IFC $_{\beta}^{\text{G}}$ irresolute mapping, since $B = \langle y, (0.3, 0.4), (0.1, 0.1) \rangle$ is an $\text{IF}_{\beta}^{\text{GOS}}$ in Y but $f^{-1}(B) = \langle x, (0.3, 0.4), (0.1, 0.1) \rangle$ is not an $\text{IF}_{\beta}^{\text{GCS}}$ in X .

Theorem 4.6: If $f : (X, \tau) \rightarrow (Y, \sigma)$ is an IFC $_{\beta}^{\text{G}}$ irresolute mapping, then f is an IF contra continuous mapping if X is an $\text{IF}_{\beta}^{\text{aT}_{1/2}}$ space.

Proof: Let A be an IFCS in Y . Then A is an $\text{IF}_{\beta}^{\text{GCS}}$ in Y . Therefore $f^{-1}(A)$ is an $\text{IF}_{\beta}^{\text{GOS}}$ in X , by hypothesis. Since X is an $\text{IF}_{\beta}^{\text{aT}_{1/2}}$ space, $f^{-1}(A)$ is an IFOS in X . Hence f is an IF contra continuous mapping.

Theorem 4.7: If $f : (X, \tau) \rightarrow (Y, \sigma)$ and $g : (Y, \sigma) \rightarrow (Z, \eta)$ are IFC $_{\beta}^{\text{G}}$ irresolute mappings, then $g \circ f : (X, \tau) \rightarrow (Z, \eta)$ is an IFC $_{\beta}^{\text{G}}$ irresolute mapping.

Proof: Let A be an $\text{IF}_{\beta}^{\text{GCS}}$ in Z . Then $g^{-1}(A)$ is an $\text{IF}_{\beta}^{\text{GOS}}$ in Y . Since f is an IFC $_{\beta}^{\text{G}}$ irresolute mapping, $f^{-1}(g^{-1}(A))$ is an $\text{IF}_{\beta}^{\text{GCS}}$ in X . That is $(g \circ f)^{-1}(A)$ is an $\text{IF}_{\beta}^{\text{GCS}}$ in X . Hence $g \circ f$ is an IFC $_{\beta}^{\text{G}}$ irresolute mapping.

Theorem 4.8: If $f : (X, \tau) \rightarrow (Y, \sigma)$ is an IFC $_{\beta}^{\text{G}}$ irresolute mapping and $g : (Y, \sigma) \rightarrow (Z, \eta)$ is an IFC $_{\beta}^{\text{G}}$ continuous mapping, then $g \circ f : (X, \tau) \rightarrow (Z, \eta)$ is an IFC $_{\beta}^{\text{G}}$ continuous mapping.

Proof: Let A be an IFCS in Z . Then by hypothesis, $g^{-1}(A)$ is an $\text{IF}_{\beta}^{\text{GOS}}$ in Y . Since f is an IFC $_{\beta}^{\text{G}}$ irresolute mapping, $f^{-1}(g^{-1}(A))$ is an $\text{IF}_{\beta}^{\text{GCS}}$ in X . That is $(g \circ f)^{-1}(A)$ is an $\text{IF}_{\beta}^{\text{GCS}}$ in X . Hence $g \circ f$ is an IFC $_{\beta}^{\text{G}}$ continuous mapping.

Theorem 4.9: If $f : (X, \tau) \rightarrow (Y, \sigma)$ is an IFC $_{\beta}^{\text{G}}$ irresolute mapping and $g : (Y, \sigma) \rightarrow (Z, \eta)$ is an IFC $_{\beta}^{\text{G}}$ continuous mapping, then $g \circ f : (X, \tau) \rightarrow (Z, \eta)$ is an IFC $_{\beta}^{\text{G}}$ continuous mapping.

Proof: Let A be an IFCS in Z . Then by hypothesis $g^{-1}(A)$ is an $\text{IF}_{\beta}^{\text{GOS}}$ in Y . Since f is an IFC $_{\beta}^{\text{G}}$ irresolute mapping, $f^{-1}(g^{-1}(A))$ is an $\text{IF}_{\beta}^{\text{GOS}}$ in X . That is $(g \circ f)^{-1}(A)$ is an $\text{IF}_{\beta}^{\text{GOS}}$ in X . Hence $g \circ f$ is an IFC $_{\beta}^{\text{G}}$ continuous mapping.

Theorem 4.10: Let $f : (X, \tau) \rightarrow (Y, \sigma)$ and $g : (Y, \sigma) \rightarrow (Z, \eta)$ be any two mappings. If the mapping $g \circ f$ is an IFC $_{\beta}^{\text{G}}$ irresolute mapping and X is an $\text{IF}_{\beta}^{\text{aT}_{1/2}}$ space, then

(i) $(g \circ f)^{-1}(B)$ is an $\text{IF}_{\beta}^{\text{GOS}}$ in X for each $\text{IF}_{\beta}^{\text{GCS}}$ in Z



- (ii) $cl((g \circ f)^{-1}(int(B))) \subseteq (g \circ f)^{-1}(B)$ for each IFS B of Z .

Proof:(i): Let B be an $IF_{\beta}^{*}GCS$ in Z . Then B^c is an $IF_{\beta}^{*}GOS$ in Z . By hypothesis, B^c is an $IF_{\beta}^{*}GCS$ in X . This implies B is an $IF_{\beta}^{*}GOS$ in X . Hence $(g \circ f)^{-1}(B)$ is an $IF_{\beta}^{*}GOS$ in X .

(ii): Let B be any IFS in Z and $int(B) \subseteq B$. Then $(g \circ f)^{-1}(int(B)) \subseteq (g \circ f)^{-1}(B)$. Since $int(B)$ is an IFOS in Z , $int(B)$ is an $IF_{\beta}^{*}GOS$ in Z . Therefore $(g \circ f)^{-1}(int(B))$ is an $IF_{\beta}^{*}GCS$ in X , by hypothesis. Since X is an $IF_{\beta}^{*}T_{1/2}$ space, $(g \circ f)^{-1}(int(B))$ is an IFCS in X . Hence $cl((g \circ f)^{-1}(int(B))) = (g \circ f)^{-1}(int(B)) \subseteq (g \circ f)^{-1}(B)$. Therefore, $cl((g \circ f)^{-1}(int(B))) \subseteq (g \circ f)^{-1}(B)$ for each IFS B of Z .

V. CONCLUSION

In this paper we introduced the notion of intuitionistic fuzzy β generalized irresolute mappings, intuitionistic fuzzy contra β generalized irresolute mapping in intuitionistic fuzzy topological space and studied some of their properties.

VI. REFERENCES

- [1] Atanassov. K., Intuitionistic fuzzy sets, 1986 ,Fuzzy Sets and Systems, 20,(Pg. 87-96).
- [2] Chang, C., Fuzzy topological spaces, 1968, J. Math. Anal. Appl., 24, , (Pg. 182-190).
- [3] Coker, D., 1997, An introduction to fuzzy topological space, Fuzzy sets and systems, 88, (Pg.81-89).
- [4] El-Shafhi, M.E., and A. Zhakari., 2007, Semi generalized continuous mappings in fuzzy topological spaces, J. Egypt. Math. Soc. 15, (Pg.157-67).
- [5] Gurcay, H., Coker, D., and Haydar, 1997, A., On fuzzy continuity in intuitionistic fuzzy topological spaces, jour. of fuzzy math., (Pg.5365-3780).
- [6] Hanafy, I.M., 2009, Intuitionistic fuzzy continuity, Canad. Math Bull. XX (Pg.1-11).
- [7] Joung Kon Jeon, Young Bae Jun, and Jin Han Park, 2005, Intuitionistic fuzzy alpha continuity and intuitionistic fuzzy pre continuity, International Journal of Mathematics and Mathematical Sciences, 19, (Pg. 3091-3101).
- [8] R.Kulandaivelu, S.Maragathavalli and K.Ramesh,2019, Intuitionistic fuzzy β generalized Continuous mappings, Int. journal of mathematics Trends and Technology, 65, (Pg.84 – 89).
- [9] K.Sakthivel,2010, "Intuitionistic Fuzzy Alpha Generalized Continuous Mappings and Intuitionistic Alpha Generalized Irresolute Mappings", Applied Mathematical Sciences 4, (Pg.1831-1842).
- [10] Seok Jong Lee and Eun Pyo Lee, 2000, The category of intuitionistic fuzzy topological spaces, Bull. Korean Math. Soc. , (Pg. 63-76).
- [11] Young Bae Jun and Seok- Zun Song, 2005,Intuitionistic fuzzy semi-pre open sets and Intuitionistic semi-pre continuous mappings, jour. of Appl. Math and computing, 19, (Pg.467-474).
- [12] Zadeh, L. A., 1965, Fuzzy sets, Information and control, 8, (Pg. 338-353).

IJEAST

INTERNATIONAL JOURNAL
OF ENGINEERING APPLIED SCIENCE
AND TECHNOLOGY

ABOUT IJEAST

International Journal of Engineering Applied Science and Technology (IJEAST) is a peer-reviewed, open access journal that publishes high-quality research papers in the field of Engineering, Applied Science and Technology.

IJEAST aims to provide a platform for researchers, academicians, and professionals to share their innovative ideas, research findings, and practical experiences with the global scientific community.

FOCUS AREAS

- Engineering
- Applied Science
- Technology
- Innovation & Development
- Interdisciplinary Studies



PEER REVIEWED

All submissions are rigorously peer reviewed to ensure quality.



OPEN ACCESS

Free and unrestricted access to research for all.



GLOBAL REACH

Connecting researchers and professionals worldwide.



TIMELY PUBLICATION

We ensure a swift and efficient publication process.



For more information, visit our website
www.ijeast.com



INTERNATIONAL JOURNAL
OF ENGINEERING APPLIED SCIENCE
AND TECHNOLOGY

✉ editor@ijeast.com

🌐 www.ijeast.com

📍 India



2455-2143